

Class: X

Subject : Maths (HAP)

Date : 12.4.18



**THEORY OF EQUATIONS**

1. If  $\alpha, \beta$  are real and  $\alpha^2, -\beta^2$  and the roots of  $a^2x^2 + x + 1 - a^2 = 0$  ( $a > 1$ ) then  $\beta^2 = \dots$   
(Ans: 1)
2. If  $K > 0$  and the product of the roots of the equation  $x^2 - 3kx + 2e^{2 \log k} - 1 = 0$  then the sum of the roots is .....  
(Ans: 6)
3. If the sum of the squares of the roots of  $x^2 + px - 3 = 0$  is 10 then the value of p is .....  
(Ans:  $\pm 2$ )
4. If  $\alpha, \beta$  are the roots of  $a(x^2 + m^2) + amx + bm^2x^2 = 0$  then  
 $a(\alpha^2 + \beta^2) + a\alpha\beta + b\beta^2\alpha^2 = \dots$   
(Ans: 0)
5. If  $\alpha, \beta$  are the roots of  $x^2 + ax - b = 0$  and  $\gamma, \delta$  are the roots of  $x^2 + ax + b = 0$  then  
 $(\alpha - \gamma)(\beta - \delta)(\alpha - \delta)(\beta - \gamma) = \dots$   
(Ans:  $4b^2$ )
6. If 8 and 2 are the roots of  $x^2 + ax + \beta = 0$  and 3, 3 are the roots of  $x^2 + \alpha x + b = 0$  then the roots of the equation  $x^2 + ax + b = 0$  are .....  
(Ans: 9, 1)
7. If  $\alpha, \beta$  are the roots of  $2x^2 + 3x - 4 = 0$  then the equation having roots  
 $2\alpha + \frac{3}{\beta}, 2\beta + \frac{3}{\alpha}$  is .....  
(Ans:  $4x^2 + 3x - 2 = 0$ )
8. If one root of  $x^2 + Kx + 27 = 0$  may be the triple the other root, then  $K = \dots$  (Ans: 12)
9. If condition that  $\sin \theta, \cos \theta$  may be roots of  $ax^2 + bx + c = 0$  is .... (Ans:  $a(a+2c)=b^2$ )
10. The maximum value of  $4x - 5x^2 - 1$  is .....  
(Ans:  $-\frac{1}{5}$ )
11. The minimum value of  $x^2 - 8x + 17, \forall x \in R$  is .....  
(Ans: 1)
12. If  $x^2 + 6x - 27 > 0, -x^2 + 3x + 4 > 0$  then  $x$  lies in the interval .... [Ans: (3,4)]
13. If  $x$  is real, then the value of  $\frac{x^2 - 3x + 4}{x^2 + 3x + 4}$  lies in the interval .... [Ans:  $(\frac{1}{7}, 7)$ ]

contd.....

14. The biquadratic equation, two of whose roots are  $1+i, 1-\sqrt{2}$  is ....

[Ans:  $(x^4 - 4x^3 + 5x^2 - 2x - 2 = 0)$ ]

15. If  $\alpha, \beta$  are the roots of  $x^2 - 2x + 4 = 0$  then  $\alpha^5 + \beta^5 = \dots\dots$  (Ans: 32)

16. If  $\alpha, \beta$  are the roots of  $x^2 - x + 1 = 0$  then  $\alpha^{2018} + \beta^{2018} = \dots\dots$  (Ans: 1)

17. If  $\alpha, \beta$  are the roots of  $9x^2 + 6x + 1 = 0$  then the equation whose roots are  $\frac{1}{\alpha}, \frac{1}{\beta}$  is  
..... (Ans:  $x^2 + 6x + 9 = 0$ )

18. If both the roots of the quadratic equation  $x^2 - 2Kx + K^2 + K - 5 = 0$  are less than 5,  
then K lies in the interval..... [Ans:  $(-\infty, 4)$ ]

19. The roots of  $3x^2 + 4x - 5 = 0$  are ..... (Ans: irrational)

20. If the roots of  $12x^2 + Kx + 5 = 0$  are in the ratio 3 : 2 then  $K = \dots\dots$  (Ans:  $\pm 5\sqrt{10}$ )

21. If  $x^2 - hx - 21 = 0, x^2 - 3hx + 35 = 0$  have a common root then  $h = \dots\dots$  (Ans:  $\pm 4$ )

22. If  $|x|^2 - 3|x| + 2 = 0$  then  $x = \dots\dots\dots$  (Ans:  $\pm 1$  or  $\pm 2$ )

23. If  $x^2 - (5m - 2)x + 4m^2 + 10m + 25 = 0$  is a perfect square, then  $K = \dots\dots$  (Ans:  $8, -\frac{4}{3}$ )

24. If  $-3 < x < 1$  then the value of  $3 - 2x - x^2$  is ..... (Ans: positive)

25. If  $a > 0$ ; and  $b^2 - 4ac = 0$  then the curve  $y = ax^2 + bx + c$  ....  
(Ans: touches the x-axis and lies above it)